### NUEN 689 PROJECT: **Deep Learning Techniques to Predict Initial Enrichment of a PWR Fuel Pin** Michael Parnell, Seray Cerezo, Course Instructor: Yang Liu, PhD Advisor: Pavel Tsvetkov

# Objective:

The objective of this project was to solve a nuclear forensics problem, determining initial U-235 enrichment based on Pu-239 produced, using different deep learning techniques. The techniques of interest were a Long Short-Term Memory (LSTM) neural network, and an Inverse Physics Informed Neural Network (IPINN).

### Background:

- The quantities, enrichments, and origins of Pu-239 are of great concern in Safeguards and Nonproliferation.
- This project aims to predict the initial uranium enrichment of some burned nuclear fuel sample, based on its Pu-239 concentration.
- Pu-239 is the most abundant plutonium isotope produced through fuel transmutation, but other nuclides (U-239, Np-239) will also be considered. Figure 1 provides a graphic of the transmutation process.
- Given data from MCNP simulations, the networks predict the initial fuel enrichment of U-235 of the sample, based on all current nuclide concentrations



## Methodology:

The LSTM NN			PII
•	This approach utilizes a Long-Short Term Memory	•	Τ
	(LSTM) NN, to understand the time-dependencies		I
	of the nuclide concentrations.		e
•	Inputs to the network will be the concentrations of		ra
	nuclides in the current sample (U-238, U-235, U-	•	Т
	239, Pu-239, Np-239), and the output will be the		fi
	estimated concentrations of those nuclides at many		a
	timesteps throughout the sample's history.		S
•	The most significant data point in this output will	•	
	be the initial U-235 enrichment.		d
			a





### **Description of Data**

MCNP data was generated for burnup simulations for seven different initial U-235 enrichments: 0.7%, 2.8%, 4%, 5%, 10%, 14%, and 20%. Concentrations of five nuclides (U-238, U-235, U-239, Pu-239, and Np-239) were available at 11 non-uniform timesteps, going up to 2 years. Reaction rates were collected for the Bateman equations in the IPINN model.



Figure 2. The fuel pin layout.

### NN

This approach relies on an inverse PINN (Physics Informed Neural Network) using the Bateman equations, which describe abundances and decay rates of the nuclides in time.

The Bateman equations used for the residual function terms, and the neural network will approximate the concentration of U-238, which is set as a learnable parameter.

The U-238 concentration can then be used to determine the enrichment of U-235 with some assumptions.

The LSTM model accurately predicts initial U-235 enrichment within 2% for each simulation, including evaluation data sets. Concentration predictions across intermediate timesteps are also generally accurate. Inverse Physics Informed Neural Network (IPINN) Results





The plots displayed are the results of the 2.8% enriched simulation. The IPINN predicted the enrichment with an average percent error of 18%. The percentage errors between the true and predicted enrichments for each simulation (for both the LSTM and IPINN models) are displayed in the table.

The LSTM model generally outperformed the IPPIN model in predicting the initial U-235 enrichment of the fuel sample. The LSTM made prediction errors that were less than 2%, but the IPPIN made prediction errors ranging from 15-25%. The LSTM model was also more flexible than the PINN; a single LSTM was capable of considering many different enrichments, but the number of IPPIN models required was equal to the number of enrichments. Future work may include a consideration of a wider range of enrichments, as well as a greater number of simulations to train the models on.

Results:

Long Short-Term Memory (LSTM) Results



## Conclusion:

L	STI	Μv	s IF	NNI	Re	sults

Nominal Simulated Enrichment (%)	True Simulated Enrichment (%)	LSTM Prediction (%) & Percent Error	IPINN Prediction (%) & Percent Error
0.7	0.8042	0.8052 (Error = 0.13%)	0.84 (Error = 20.00%)
2.8	3.241	3.245 (Error = 0.14%)	3.32 (Error = 18.57%)
4.0	4.597	4.533 (Error = 1.39%)	4.69 (Error = 17.25%)
5.0	5.741	5.698 (Error = 0.74%)	5.85 (Error = 17.00%)
10	11.48	11.68 (Error = 1.75%)	11.6 (Error = 16.00%)
14	17.20	17.42 (Error = 1.32%)	17.4 (Error = 24.29%)
20	22.92	22.76 (Error = 0.69%)	23.1 (Error = 15.50%)



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